



**AFRL-ML-WP-TP-2007-501**

**INVESTIGATION OF THE SELF-PUMPED TWO-BEAM  
COUPLING IN A PHOTOREFRACTIVE MATERIAL  
USING BEAM PROPAGATION SIMULATION (Preprint)**

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Hardened Materials Branch  
Survivability and Sensor Materials Division**

**JANUARY 2006**

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*Form Approved  
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<b>1. REPORT DATE (DD-MM-YY)</b> January 2006			<b>2. REPORT TYPE</b> Conference Paper Preprint		<b>3. DATES COVERED (From - To)</b>	
<b>4. TITLE AND SUBTITLE</b>  INVESTIGATION OF THE SELF-PUMPED TWO-BEAM COUPLING IN A PHOTOREFRACTIVE MATERIAL USING BEAM PROPAGATION SIMULATION (Preprint)					<b>5a. CONTRACT NUMBER</b> IN-HOUSE <b>5b. GRANT NUMBER</b> <b>5c. PROGRAM ELEMENT NUMBER</b> 62102F	
<b>6. AUTHOR(S)</b>  D.R. Evans, G. Cook, J. L. Carns, and M. A. Saleh, (Agile Filters Project, Exploratory Development) P. P. Banerjee (University of Dayton)					<b>5d. PROJECT NUMBER</b> 4348 <b>5e. TASK NUMBER</b> RG <b>5f. WORK UNIT NUMBER</b> M03R1000	
<b>7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES)</b>  Agile Filters Project, Exploratory Development Hardened Materials Branch, Survivability and Sensor Materials Division Materials and Manufacturing Directorate, Air Force Research Laboratory Wright-Patterson Air Force Base, OH 45433-7750 Air Force Materiel Command, United States Air Force			University of Dayton Dayton, OH		<b>8. PERFORMING ORGANIZATION REPORT NUMBER</b>  AFRL-ML-WP-TP-2007-501	
<b>9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES)</b>  Air Force Research Laboratory Materials and Manufacturing Directorate Wright-Patterson Air Force Base, OH 45433-7750 Air Force Materiel Command United States Air Force					<b>10. SPONSORING/MONITORING AGENCY ACRONYM(S)</b> AFRL/MLPJ <b>11. SPONSORING/MONITORING AGENCY REPORT NUMBER(S)</b> AFRL-ML-WP-TP-2007-501	
<b>12. DISTRIBUTION/AVAILABILITY STATEMENT</b> Approved for public release; distribution unlimited.						
<b>13. SUPPLEMENTARY NOTES</b> The U.S. Government is joint author of this work and has the right to use, modify, reproduce, release, perform, display, or disclose the work. PAO case number AFRL/WS 06-0313, 07 February 2006. Submitted to the proceedings of the Third International Photorefractive Workshop, sponsored by AFRL/MLPJ. This is the best quality available.						
<b>14. ABSTRACT</b> <ul style="list-style-type: none"> <li>• At this point we are capable of stimulating the self-pumped contra-directional two-beam coupling in a photorefractive medium with arbitrary shaped beams.</li> <li>• Our simulation shows positive role of the photovoltaic effect in self-pumped contra-directional TBC, in agreement with experimental observation.</li> </ul>						
<b>15. SUBJECT TERMS</b> Two-Beam Coupling, Beam Propagation, Photorefractive						
<b>16. SECURITY CLASSIFICATION OF:</b>			<b>17. LIMITATION OF ABSTRACT:</b> SAR	<b>18. NUMBER OF PAGES</b> 14	<b>19a. NAME OF RESPONSIBLE PERSON</b> (Monitor) Dean R. Evans, Ph.D. <b>19b. TELEPHONE NUMBER</b> (Include Area Code) (937) 255-4588	

Standard Form 298 (Rev. 8-98)  
Prescribed by ANSI Std. Z39-18

# Investigation of the self-pumped two-beam coupling in a photorefractive material using beam propagation simulation



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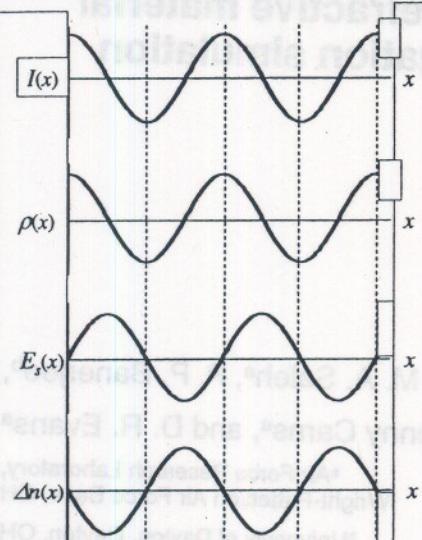
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## Outline

- Photorefractive two-beam coupling
- Motivation of this work
- Beam propagation method
- Simulation results
- Conclusions



## Diffusion Model of Photorefraction



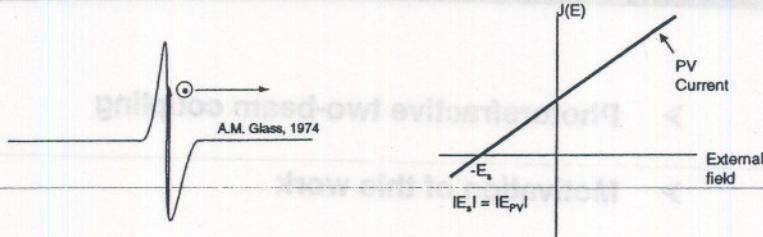
- Two plane waves interfere to produce the spatially modulated intensity.
- The generated free charge carriers diffuse to create the spatially varying charge distribution, which, in turn gives rise to an electrostatic field distribution that is 90-degree phase shifted.
- The refractive index variation is produced through the linear electro-optic effect.
- Can be summarized by this simplified expression<sup>1</sup>

$$\Delta n = c_{df} E_{\infty} \propto \nabla I(x, y, z)$$

J. J. Liu and P. P. Banerjee, J. Opt. Soc. Am. B, 11, pp. 1688-1693, 1994



## Photovoltaic Effect



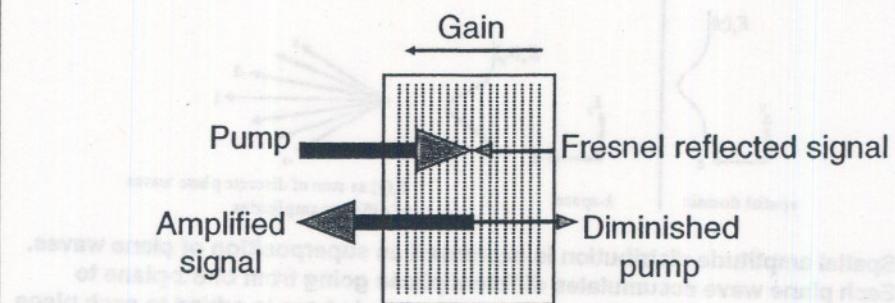
- In addition to the diffusion process, some anisotropic crystals (i.e., LiNbO<sub>3</sub>) exhibit strong photovoltaic effect which refers to the tendency of the photo-ionization process (under uniform illumination) to eject the electron in a preferred direction due to the asymmetric potential in the anisotropic crystal.

$$\Delta n = c_{PV} E_{\infty} \propto I(x, y, z)$$

- Resulting current flow can be opposed by applying an external E-field.
- In the closed circuit condition the photocurrent will equal zero at -E<sub>s</sub>, the effects of the PV and ext. E-field cancel out.
- Under open circuit condition it is generally assumed that the bulk field cancels out the photovoltaic field and PV effect does not assist TBC.



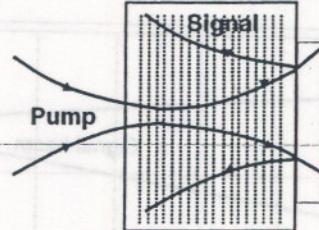
## Contra-directional Self-pumped Two-beam coupling



Periodic index modulation from the photorefractive effect can be used to couple energy between two interfering beams. One novel variation of the contra-directional beam coupling is the self-pumped beam-coupling where the signal beam is generated by the Fresnel reflection of the pump.



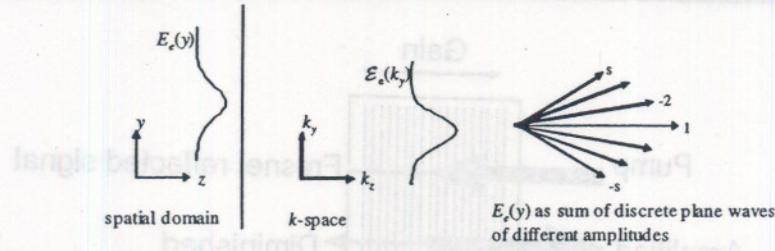
## Motivation and goals



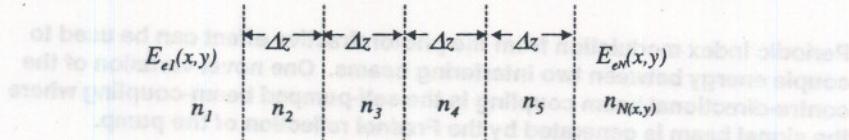
- Strong dependence of the TBC efficiency on the spot size is observed, attributed to diffraction and the resulting change in the spatial overlaps.
- The goal of our simulation:
  - is to simulate arbitrary shaped beam-coupling using exact diffraction.
  - is to analyze the contribution from photovoltaic effect and diffusion in two-beam coupling.
- To the best of our knowledge, self-pumped contra-directional TBC has not been done with BPM.



## Split-step Beam Propagation



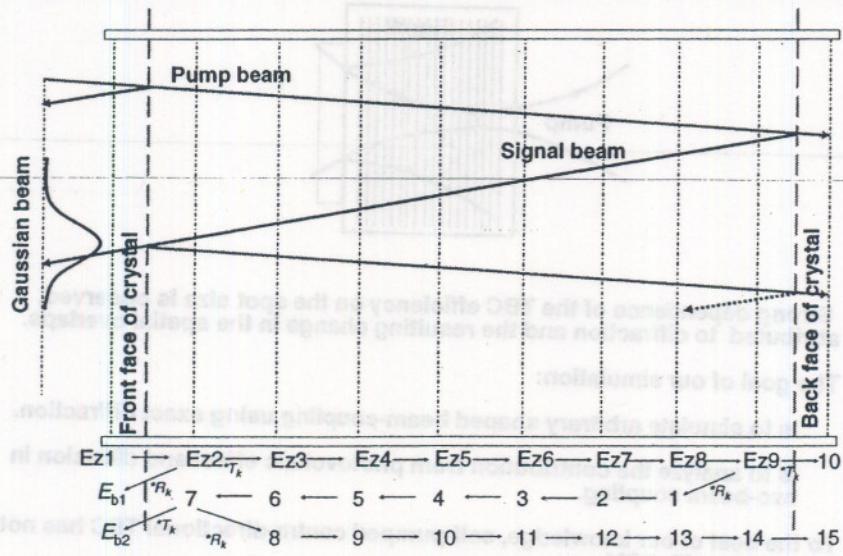
Spatial amplitude distribution is expressed as superposition of plane waves. Each plane wave accumulates different phase going from one  $z$ -plane to another  $z$ -plane. After a distance  $\Delta z$  accumulated phase is added to each plane wave and the spatial amplitude distribution can be recalculated again.



The optical path is broken into a sequence of finite steps.

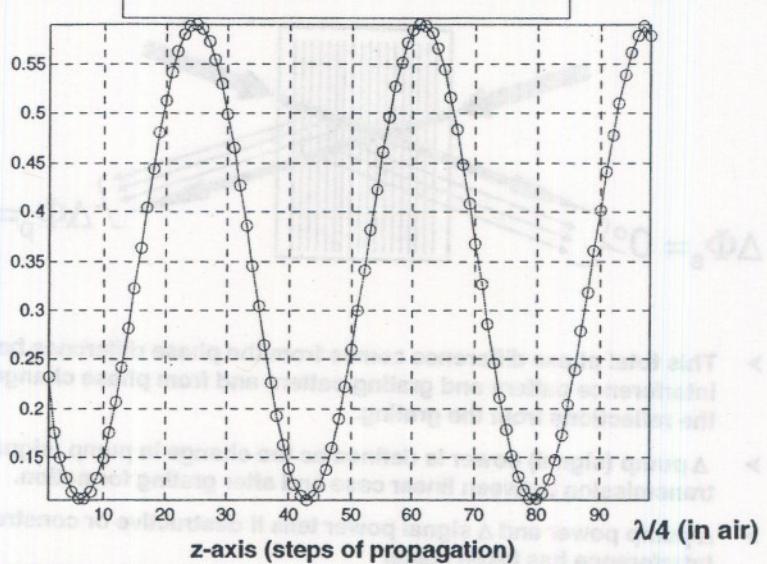


## Schematic





## Simulated Interference



## Steps of simulation



- We simulate the interference of the beams by adding the forward and backward propagating beams at every incremental  $z$  value. This produces the modulated  $I(z)$  inside the crystal.
- We use this modulated intensity to calculate the space charge field. Change in Index then can be calculated from the electro-optic effect.
- We modify the index inside the crystal by using the simplified expression<sup>1</sup> (omitting the details of space charge field generation):

$$n = n_0 + \Delta n, \quad \text{where} \quad \Delta n = c_{PV} E_{sc} \propto I(x, y, z) \quad (\text{PV})$$

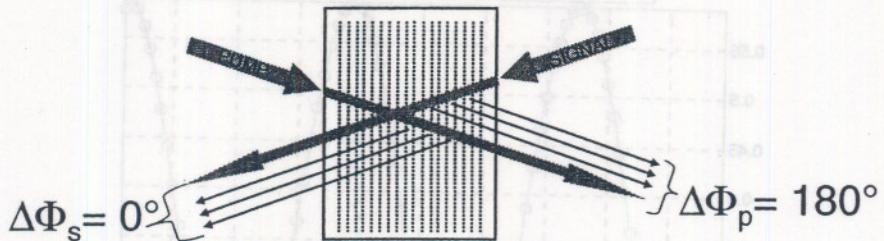
or,  $\Delta n = c_{df} E_{sc} \propto \nabla I(x, y, z) \quad (\text{diffusion})$

- For this work only a  $\lambda$  long crystal was simulated. We chose the two constants such that there was observable beam coupling in this thin crystal and the  $\Delta n$  is same for both diffusion and PV effect.

J. J. Liu and P. P. Banerjee, *J. Opt. Soc. Am. B.* 11, pp. 1688-1693, 1994<sup>1</sup>.



## Condition for Beam coupling



- This total phase difference comes from the phase difference between interference pattern and grating pattern and from phase change due to the reflections from the grating.
- $\Delta$  pump (signal) power is defined as the change in pump (signal) transmission between linear case and after grating formation.
- $\Delta$  pump power and  $\Delta$  signal power tells if destructive or constructive interference has taken place.



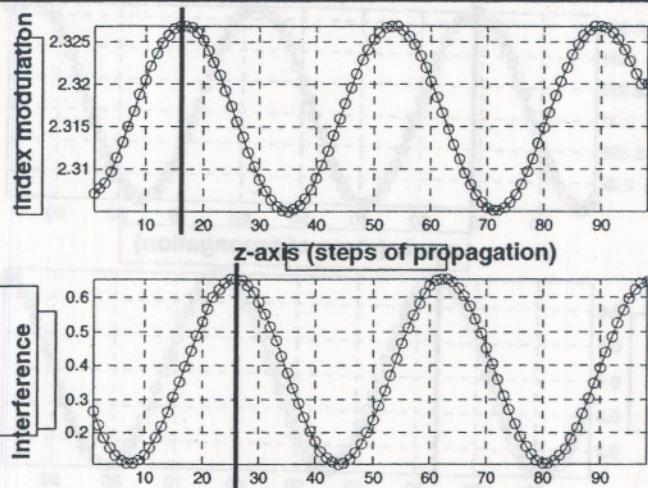
## Steps of convergence



- For a given intensity distribution  $I(x,y,z)$  inside the crystal, we calculate  $n(x,y,z)$ .
- We obtain a new intensity distribution  $I(x,y,z)$  through another round of beam propagation, where pump and signal scatters are also accounted for, which gives us a new  $n(x,y,z)$ .
- Error is defined as the average percent difference between successive interference amplitude arrays.
- We continue the process until we obtain a converged steady state solution for both  $I(x,y,z)$  and  $n(x,y,z)$  using iterative shooting method.
- For the converged  $I(x,y,z)$  and  $n(x,y,z)$  pump and signal scatters are added to signal and pump respectively and the power changes due to the interference are calculated.



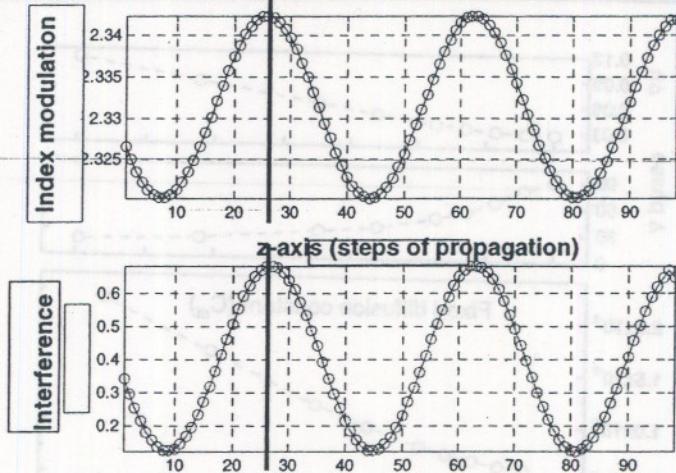
## Considering diffusion alone



The index and interference are 90-degree out of phase (as expected).  $\Delta n = 0.022$  (for  $C_{df} = 0.27$ ).  $\Delta P = 0.58\%$  of pump power.  $C_{df} = -0.27$  (equivalent to rotating optic axis  $180^\circ$ ) makes  $\Delta P = -0.58\%$  of pump power.



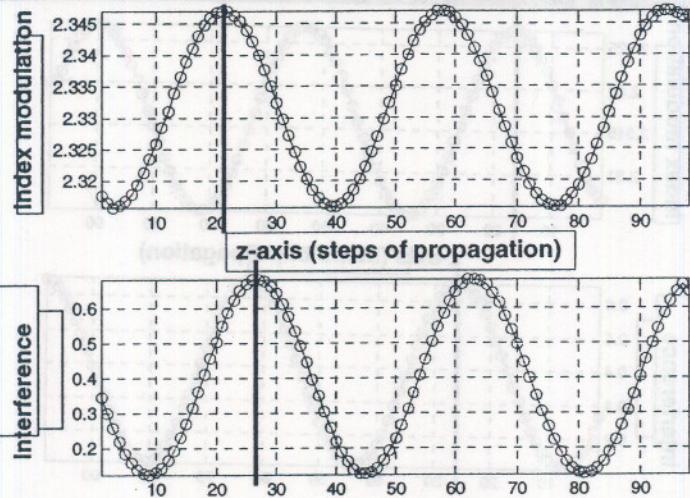
## Considering PV alone



The index and interference are in phase as expected.  $\Delta n = 0.022$ . ( $C_{pv}$  Chosen to match  $\Delta n$ ). Diffraction—not beam-coupling observed. Reversal of the crystal direction does not affect the direction of power flow.



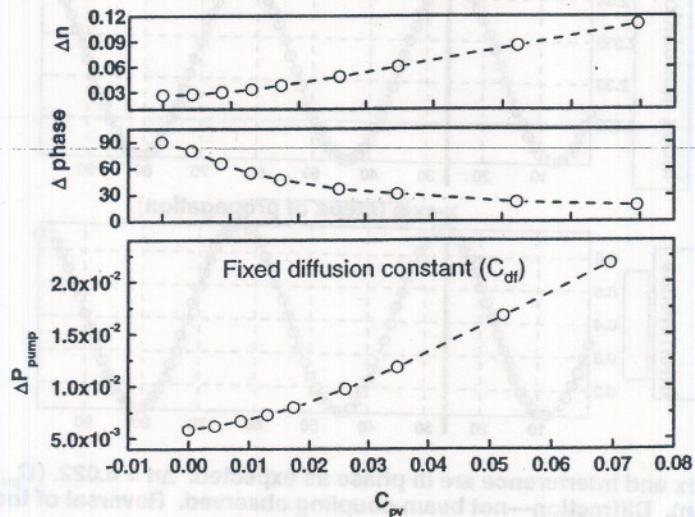
## Considering both PV and Diffusion



Phase difference > 0 and < 90 deg.  $\Delta n = 0.031$ , larger than considering them alone.  $\Delta P$  changes with PV contribution.

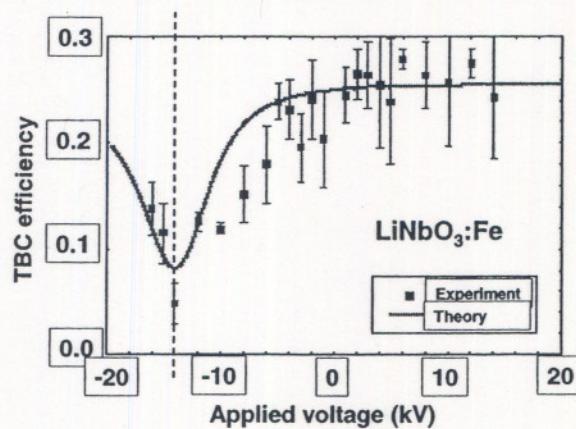


## Photovoltaic Contribution





## Observed photovoltaic contribution



G. Cook, J. P. Duignan, D. C. Jones, "Photovoltaic contribution to counter-propagating two-beam coupling in photorefractive lithium niobate" Optics communications, vol. 192, pp 393-398, 2001.

$$E_s = \frac{E_0 + iE_D + E_{PV}}{1 + E_D/E_Q - i(E_0/E_Q + (N_A/N_D)(E_{PV}/E_Q))}$$



## Conclusions and Future Work



- At this point we are capable of simulating the self pumped contra-directional two-beam coupling in a photorefractive medium with arbitrary shaped beams.
- Our simulation shows positive role of the photovoltaic effect in self-pumped contra-directional TBC, in agreement with experimental observation.
- A more complete simulation that includes dark conductivity and un-simplified space charge field is in progress.